## **4725 Further Pure Mathematics 1**

| 1. |   | B1     |               | State correct value of $S_{250}$ or $S_{100}$            |
|----|---|--------|---------------|--|
|    |   | M1     | _             | Subtract $S_{250} - S_{100}$ (or $S_{101}$ or $S_{99}$ ) |
|    | 984390625 - 25502500 = 958888125          | A1     | 3<br><b>3</b> | Obtain correct exact answer                              |
| 2. | 3a + 5b = 1, a + 2b = 1                   | M1     | 3             | Obtain a pair of simultaneous                            |
|    | 34 130 -1, 4 1 25 -1                      | M1     |               | equations  |
|    | a = -3, b = 2                             | A1 A1  | 4             | Attempt to solve   |
|    |   |        | 4             | Obtain correct answers.                                  |
| 3. | (i) 11 – 29i                              | B1 B1  | 2             | Correct real and imaginary parts                         |
|    | (ii) 1 + 41i                              | B1 B1  | 2<br><b>4</b> | Correct real and imaginary parts                         |
| 4. | Either $p + q = -1, pq = -8$              | B1     |               | Both values stated or used                               |
|    | $\frac{p+q}{pq}$                          | B1     |               | Correct expression seen                                  |
|    |   | M1     |               | Use their values in their expression                     |
|    | $-\frac{7}{8}$                            | A1     | 4             | Obtain correct answer                                    |
|    | 0   |        | 4             |  |
|    | 0, 1,1,2                                  | B1     |               | Substitute $x = \frac{1}{u}$ and use new                 |
|    | $Or \qquad \frac{1}{p} + \frac{1}{q} = 8$ |        |               | quadratic  |
|    | p+q=1                                     | B1     |               | Correct value stated                                     |
|    | 7   | M1     |               | Use their values in given expression                     |
|    | $-\frac{7}{8}$                            | A1     |               | Obtain correct answer                                    |
|    |   | 711    |               | Obtain correct answer                                    |
|    | Or $\frac{-1\pm\sqrt{33}}{2}$             | M1     |               | Find roots of given quadratic                            |
|    | Or $\frac{1\pm\sqrt{33}}{2}$              |        |               | equation   |
|    | <del>-</del>                              | A1     |               | Correct values seen                                      |
|    | $-\frac{7}{8}$                            | M1     |               | Use their values in given expression                     |
|    |   | A1     |               | Obtain correct answer                                    |
| 5. | (i) $u^3 = \{(-)(5u+7)\}^2$               | M1     |               | Use given substitution and rearrange                     |
|    |   | A1     |               | Obtain correct expression, or                            |
|    |   |        |               | equivalent   |
|    | $u^3 - 25u^2 - 70u - 49 = 0$              | A1     | 3             | Obtain correct final answer                              |
|    |   |        |               |  |
|    | (ii)                                      | M1     |               | Use coefficient of $u$ of their cubic or                 |
|    |   |        |               | identity connecting the symmetric                        |
|    |   |        |               | functions and substitute values from                     |
|    | 70  | A 1 f4 | 2             | given equation   |
|    | -70                                       | A1 ft  | 2<br><b>5</b> | Obtain correct answer                                    |
|    |   |        | 3             |  |

| 6. | (i) $3\sqrt{2}, -\frac{\pi}{4} \text{ or } -45^{\circ} \text{ AEF}$ | B1 B1 | 2  | State correct answers                       |
|----|---|-------|----|---|
|    | 4   |       |    |   |
|    | (ii)(a)   | B1B1  | 3  | Circle, centre (3, -3),                     |
|    |   | B1 ft |    | through $O$ ft for $(\pm 3, \pm 3)$ only    |
|    | (ii)(b)   | B1    |    | Straight line with +ve slope,               |
|    |   | B1    | 3  | through (3, -3) or their centre             |
|    |   | B1    |    | Half line only starting at centre           |
|    | (iii)   | B1ft  |    | Area above horizontal through $a$ ,         |
|    |   | B1ft  |    | below (ii) (b)                              |
|    |   | B1ft  | 3  | Outside circle                              |
|    |   |       | 11 |   |
| 7. | (i)   | M1    | 2  | Show that terms cancel in pairs             |
|    |   | A1    | 2  | Obtain given answer correctly               |
|    | (ii)  | M1    |    | Attempt to expand and simplify              |
|    |   | A1    | 2  | Obtain given answer correctly               |
|    |   | 54.54 |    |   |
|    | (iii)   | B1 B1 |    | Correct $\sum r$ stated $\sum 1 = n$        |
|    |   |       |    |   |
|    |   | M1*   |    | Consider sum of 4 separate terms on         |
|    |   | *DM1  |    | RHS Required sum is LHS – 3 terms           |
|    | ( 1)4 1 ( 1)(2 1) 2 ( 1)  | A1    |    |   |
|    | $(n+1)^4 - 1 - n(n+1)(2n+1) - 2n(n+1) - n$                          | AI    |    | Correct unsimplified expression             |
|    | n   |       |    |   |
|    | $4\sum_{r=1}^{n} r^3 = n^2 (n+1)^2$                                 | A1    |    | Obtain given answer correctly               |
|    | r=1   | 711   | 6  | Obtain given answer correctly               |
| 8. | (i)   | B1    | 10 | Find coordinates (0, 0) (3, 1) (2, 1)       |
| 0. | (1)   | B1    |    | (5, 2) found                                |
|    |   | B1    | 3  | Accurate diagram sketched                   |
|    | $\begin{pmatrix} 1 & 0 \\ 1 & 1 \end{pmatrix}$                      |       |    |   |
|    | $\begin{pmatrix} \begin{pmatrix} 1 & 1 \end{pmatrix} \end{pmatrix}$ | B1 B1 | 2  | Each column correct                         |
|    | (iii) Either  | B1    |    | Correct inverse for their (ii) stated       |
|    | $(1 \ 2)$   | M1    |    | Post multiply <b>C</b> by inverse of (ii)   |
|    | $\begin{pmatrix} 0 & 1 \end{pmatrix}$                               |       |    |   |
|    | (* -)   | A1ft  |    | Correct answer found                        |
|    | Or  | M1    |    | Set up 4 equations for elements from        |
|    |   | 1,11  |    | correct matrix multiplication               |
|    |   | A2ft  |    | All elements correct, -1 each error         |
|    |   | B1    |    | Shear,                                      |
|    |   | B1    |    | x axis invariant or parallel to x-axis      |
|    |   | B1    | 6  | eg image of $(1, 1)$ is $(3, 1)$            |
|    |   |       | 11 | <b>SR</b> allow s.f. 2 or shearing angle of |
|    |   |       |    | correct angle to appropriate axis           |

| 9.  | $\begin{vmatrix} a & 1 \end{vmatrix} \begin{vmatrix} 1 & 1 \end{vmatrix} \begin{vmatrix} 1 & a \end{vmatrix}$                                      | M1    |    | Correct expansion process shown                |
|-----|--|-------|----|--|
|     | (i) $a \begin{vmatrix} a & 1 \\ 1 & 2 \end{vmatrix} - \begin{vmatrix} 1 & 1 \\ 1 & 2 \end{vmatrix} + \begin{vmatrix} 1 & a \\ 1 & 1 \end{vmatrix}$ | A1    |    | Obtain correct unsimplified                    |
|     |  |       |    | expression                                     |
|     | $2a^{2}-2a$  | A1    | 3  |  |
|     |  |       |    | Obtain correct answer                          |
|     | (ii)   | M1    |    |  |
|     | a = 0  or  1   | A1ft  |    | Equate their det to 0                          |
|     |  | A1ft  | 3  | Obtain correct answers, ft solving a quadratic |
|     | (iii) (a)  | B1 B1 |    | Equations consistent, but non unique solutions |
|     | (b)  | B1    |    | Correct equations seen &                       |
|     |  | B1    | 4  | inconsistent, no solutions                     |
|     |  |       | 10 |  |
| 10. | i)   | M1    |    | Attempt to find next 2 terms                   |
|     | $u_2 = 7  u_3 = 19$  | A1    | _  | Obtain correct answers                         |
|     |  | A1    | 3  | Show given result correctly                    |
|     | (ii)   | M1    |    | Expression involving a power of 3              |
|     | $u_n = 2(3^{n-1}) + 1$   | A1    | 2  | Obtain correct answer                          |
|     | (iii)  | B1ft  |    | Verify result true when $n = 1$ or $n = 2$     |
|     |  | M1    |    | Expression for $u_{n+1}$ using recurrence      |
|     | $u_{n+1} = 3(2(3^{n-1})+1) - 2$  |       |    | relation                                       |
|     |  | A1    |    | Correct unsimplified answer                    |
|     | $u_{n+1} = 2(3^n) + 1$   | A1    |    | Correct answer in correct form                 |
|     |  | B1    |    | Statement of induction conclusion              |
|     |  |       | 5  |  |
|     |  |       | 10 |  |